

## 1YGB - MP2 PAPER P - QUESTION 1

a) LOOKING AT THE PICTURE OPPOSITE

• AREA OF SECTOR  $\overset{D}{\curvearrowright} \overset{C}{\curvearrowleft} \overset{A}{\curvearrowright} = \frac{1}{2} r^2 \theta$

$$= \frac{1}{2} \times 10^2 \times 1.2708\dots$$

$$= \underline{\underline{63.5398}}$$

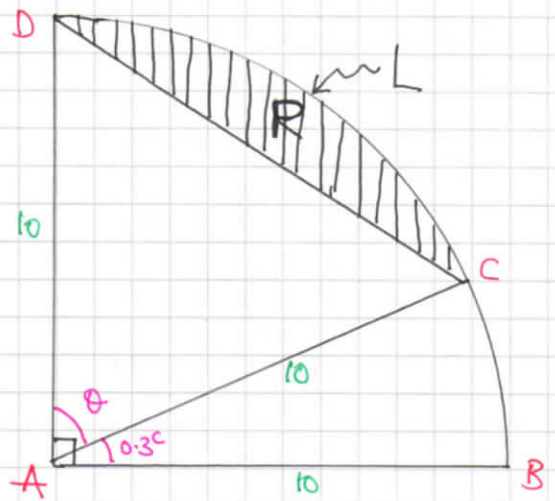
• AREA OF  $\triangle ACD = \frac{1}{2} |AD| |AC| \sin \theta$

$$= \frac{1}{2} \times 10 \times 10 \times \sin(1.2708\dots)$$

$$= \underline{\underline{47.7668\dots}}$$

• AREA OF R =  $63.5398\dots - 47.7668\dots$

$$\approx \underline{\underline{15.8 \text{ cm}^2}}$$



$$\theta = \frac{\pi}{2} - 0.3^\circ$$

$$\theta = 1.2708\dots$$

b) BY THE COSINE RULE ON  $\triangle ACD$

$$|DC|^2 = |DA|^2 + |AC|^2 - 2|DA||AC|\cos\theta$$

$$|DC|^2 = 10^2 + 10^2 - 2 \times 10 \times 10 \times \cos(1.2708\dots)$$

$$|DC|^2 = 200 - 200 \cos(1.2708\dots)$$

$$|DC|^2 = 140.89666\dots$$

$$|DC| = 11.869\dots$$

USING THE ARCLENGTH FORMULA

$$L = r\theta$$

$$L = 10 \times 1.2708\dots$$

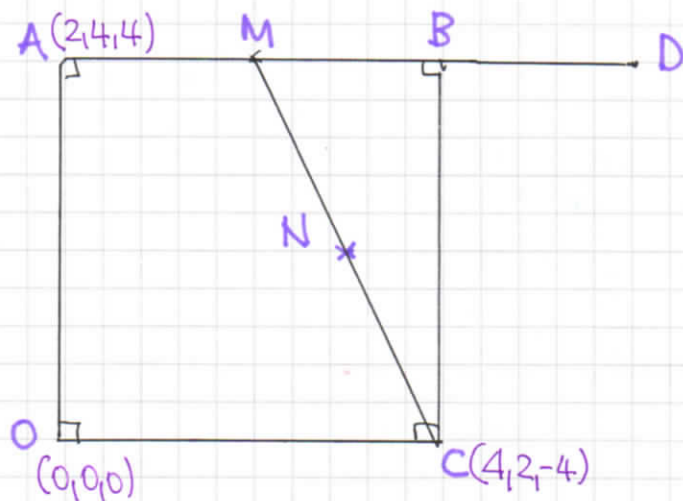
$$L = 12.708\dots$$

THENCE THE PERIMETER OF R IS  $11.869\dots + 12.708\dots \approx \underline{\underline{24.6 \text{ cm}}}$

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1YGB - MP2 PAPER P - QUESTION 2

a) STARTING WITH A DIAGRAM FOR THE SQUARE



$$\bullet \vec{OB} = \vec{OA} + \vec{AB}$$

$$\vec{OB} = \vec{OA} + \vec{OC}$$

$$\vec{OB} = (2,4,4) + (4,2,-4)$$

$$\vec{OB} = (6,6,0)$$

$$\therefore \underline{\underline{b = 6i + 6j}}$$

$$\bullet \vec{OD} = \vec{OA} + \vec{AD}$$

$$\vec{OD} = \vec{OA} + \frac{3}{2} \vec{AB}$$

$$\vec{OD} = \vec{OA} + \frac{3}{2} \vec{OC}$$

$$\vec{OD} = (2,4,4) + \frac{3}{2}(4,2,-4)$$

$$\vec{OD} = (8,7,-2)$$

$$\therefore \underline{\underline{d = 8i + 7j - 2k}}$$

$$\bullet \vec{ON} = \vec{OC} + \frac{1}{2} \vec{CM}$$

$$\vec{ON} = \vec{OC} + \frac{1}{2} [\vec{CO} + \vec{OA} + \frac{1}{2} \vec{AB}]$$

$$\vec{ON} = \vec{OC} + \frac{1}{2} \vec{CO} + \frac{1}{2} \vec{OA} + \frac{1}{4} \vec{AB}$$

$$\vec{ON} = (4,2,-4) + \frac{1}{2}(-4,-2,4) + \frac{1}{2}(2,4,4) + \frac{1}{4} \vec{OC}$$

$$\vec{ON} = (4,2,-4) + (-2,-1,2) + (1,2,2) + \frac{1}{4}(4,2,-4)$$

1YGB - MP2 PAPER P - QUESTION 2

$$\vec{ON} = (3, 3, 0) + (1, \frac{1}{2}, -1)$$

$$\vec{ON} = (4, \frac{7}{2}, -1)$$

$$\therefore \underline{n = 4i + \frac{7}{2}j - k}$$

b) COMPARING VECTORS FOUND ABOVE

$$\vec{OD} = 8i + 7j - 2k$$

$$\vec{OD} = 2(4i + \frac{7}{2}j - k)$$

$$\vec{OD} = 2\vec{ON}$$

$\therefore O, N, D$  ARE COLLINEAR

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1YGB - MP2 PAPER P - QUESTION 3

$$|2x+1| + 9 < 4x$$

REWRITE AS

$$|2x+1| + 9 < 4x$$

$$|2x+1| < 4x - 9$$

SOLVE THE CORRESPONDING EQUATION TO FIND CRITICAL VALUES

$$2x+1 = 4x-9$$

$$10 = 2x$$

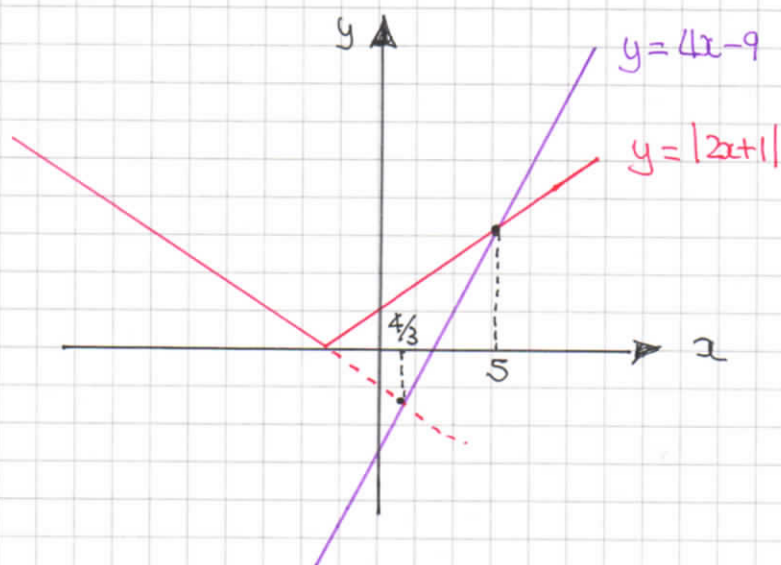
$$x = 5$$

$$2x+1 = -4x+9$$

$$6x = 8$$

$$x = \frac{4}{3}$$

SKETCHING  $y = |2x+1|$  &  $y = 4x-9$  IN THE SAME AXES



FROM THE GRAPH WE OBTAIN  $x > 5$  (BY LOOKING AT  $|2x+1| < 4x-9$ )

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# YGB - MP2 PAPER P - QUESTION 4

a) FORMING THE DIFFERENTIAL EQUATION FROM THE INFORMATION GIVEN

$$\frac{dH}{dt} = +k(12-H)$$

Annotations:  
-  $\frac{dH}{dt}$ : RATE (with an upward arrow)  
-  $+$ : INCREASE (with an upward arrow)  
-  $k$ : PROPORTIONAL (with an upward arrow)  
-  $(12-H)$ : HEIGHT (with an upward arrow)  
-  $12$ : MAX HEIGHT (with a blue arrow pointing to it)

$H$  = height of tree (m)  
 $t$  = time (months)

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$H_{\text{MAX}} = 12\text{m}$

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$t = 0$   
 $H = 1$

$\left. \frac{dH}{dt} \right|_{\substack{t=0 \\ H=1}} = 0.1$

● APPLY CONDITION  $\left. \frac{dH}{dt} \right|_{H=1} = 0.1$

$$0.1 = k(12-1)$$

$$k = \frac{1}{110}$$

●  $\frac{dH}{dt} = \frac{1}{110}(12-H)$

$110 \frac{dH}{dt} = 12-H$  ~~AS REQUIRED~~

b) SOLVING THE O.D.E. BY SEPARATING VARIABLES

$$\Rightarrow 110 dH = (12-H) dt$$

$$\Rightarrow \frac{110}{12-H} dH = 1 dt$$

$$\Rightarrow \int \frac{110}{12-H} dH = \int 1 dt$$

$$\Rightarrow -110 \ln|12-H| = t + C$$

$$\Rightarrow \ln|12-H| = -\frac{1}{110}t + C$$

$$\Rightarrow 12-H = e^{-\frac{1}{110}t + C}$$

YGB - MP2 PAPER P - QUESTION 4

$$\Rightarrow 12 - H = e^{-\frac{1}{110}t} \times e^c$$

$$\Rightarrow 12 - H = A e^{-\frac{1}{110}t} \quad (A = e^c)$$

$$\Rightarrow H = 12 + A e^{-\frac{1}{110}t}$$

APPLY THE CONDITION  $t=0$   $H=1$

$$\Rightarrow 1 = 12 + A$$

$$\Rightarrow A = -11$$

$$\therefore H = 12 - 11 e^{-\frac{1}{110}t}$$

c) WHEN  $t=60$  (5 YEARS = 60 MONTHS)

$$\Rightarrow H = 12 - 11 e^{-\frac{1}{110} \times 60}$$

$$\Rightarrow H = 12 - 11 e^{-\frac{6}{11}}$$

$$\Rightarrow H \approx 5.62 \text{ m}$$

d) WHEN  $H=11$

$$\Rightarrow 11 = 12 - 11 e^{-\frac{1}{110}t}$$

$$\Rightarrow 11 e^{-\frac{1}{110}t} = 1$$

$$\Rightarrow e^{-\frac{1}{110}t} = \frac{1}{11}$$

$$\Rightarrow e^{\frac{1}{110}t} = 11$$

$$\Rightarrow \frac{1}{110}t = \ln 11$$

$$\Rightarrow t = 110 \ln 11 \approx 263.76 \dots \text{ months} \xrightarrow{\div 12} \approx 22 \text{ YEARS}$$

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## 1Y6B - MP2 PAPER P - QUESTION 5

a) FORMING TWO EQUATIONS FROM THE INFORMATION GIVEN

$$\bullet S_2 = 40$$

$$\Rightarrow a + (a+d) = 40$$

$$\Rightarrow 2a + d = 40$$

$$\bullet S_4 = 130$$

$$\Rightarrow a + (a+d) + (a+2d) + (a+3d) = 130$$

$$\Rightarrow 4a + 6d = 130$$

$$\Rightarrow 2a + 3d = 65$$

SUBTRACTING

$$2a + 3d = 65$$

$$2a + d = 40$$

$$\hline 2d = 25$$

$$\underline{d = 12.5}$$

q

$$2a + d = 40$$

$$2a + 12.5 = 40$$

$$2a = 27.5$$

$$\underline{a = 13.75}$$

∴ using  $S_n = \frac{n}{2} [2a + (n-1)d]$

$$S_5 = \frac{5}{2} [2 \times 13.75 + 4 \times 12.5]$$

$$\underline{S_5 = 193.75}$$

b) REPEATING BEST FOR A GEOMETRIC PROGRESSION NOTICE  $S_4 = \frac{a(r^4-1)}{r-1}$

$$\bullet S_2 = 40$$

$$\Rightarrow a + ar = 40$$

$$\Rightarrow a(1+r) = 40$$

$$\bullet S_4 = 130$$

$$\Rightarrow \frac{a(r^4-1)}{r-1} = 130$$

$$\Rightarrow \frac{a(r^2-1)(r^2+1)}{r-1} = 130$$

$$\Rightarrow \frac{a(r+1)(r-1)(r^2+1)}{(r-1)} = 130$$

As  $r-1 \neq 0$  WE MAY CANCEL

$$\Rightarrow a(r+1)(r^2+1) = 130$$

$$\Rightarrow 40(r^2+1) = 130$$

1YGB - MP2 PAPER P - QUESTION 5

$$\Rightarrow r^2 + 1 = \frac{13}{4}$$

$$\Rightarrow r^2 = \frac{9}{4}$$

$$\Rightarrow r = \begin{cases} \frac{3}{2} \\ -\frac{3}{2} \end{cases}$$

Now if  $r = \frac{3}{2}$

$$a = \frac{40}{1+r}$$

$$a = \frac{40}{1+\frac{3}{2}}$$

$$a = \frac{40}{2.5}$$

$$a = 16$$

$$\sum_{t=1}^5 P_t = \frac{16(1.5^5 - 1)}{1.5 - 1}$$

$$\underline{\underline{\sum_{t=1}^5 P_t = 211}}$$

AND if  $r = -\frac{3}{2}$

$$a = \frac{40}{1+r}$$

$$a = \frac{40}{1-\frac{3}{2}}$$

$$a = \frac{40}{-0.5}$$

$$a = -80$$

$$\sum_{t=1}^5 P_t = \frac{-80((-1.5)^5 - 1)}{-1.5 - 1}$$

$$\underline{\underline{\sum_{t=1}^5 P_t = -275}}$$

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## 1Y6B - MP2 PAPER P - QUESTION 6

a) START BY DIFFERENTIATION

$$y = \frac{x+1}{x^3+2x+1} \Rightarrow \frac{dy}{dx} = \frac{(x^3+2x+1) \times 1 - (x+1)(3x^2+2)}{(x^3+2x+1)^2}$$

$$\Rightarrow \frac{dy}{dx} = \frac{x^3+2x+1 - (3x^3+3x^2+2x+2)}{(x^3+2x+1)^2}$$

$$\Rightarrow \frac{dy}{dx} = \frac{-2x^3-3x^2-1}{(x^3+2x+1)^2}$$

SOLVING FOR ZERO TO SEARCH FOR STATIONARY POINTS

$$\Rightarrow -2x^3-3x^2-1=0$$

$$\Rightarrow -3x^2-1=2x^3$$

$$\Rightarrow -\frac{3x^2+1}{2x^2}=x$$

AS REQUIRED

b) USING THE ABOVE FORMULA AS A RECURRENCE RELATION

$$x_{n+1} = -\frac{3x_n^2+1}{2x_n^2}, \quad \begin{aligned} x_1 &= -1.7 \\ x_2 &= -1.67301\dots \\ x_3 &= -1.67864\dots \\ x_4 &= -1.67744\dots \\ x_5 &= -1.67769 \\ x_6 &= -1.67764 \\ x_7 &= -1.67765 \end{aligned}$$

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## LYGB - MP2 PAPER P - QUESTION 6

NOW USING  $x_7 = -1.67765...$  WE OBTAIN

$$y = \frac{x_7 + 1}{(x_7)^3 + 2x_7 + 1} = 0.095753...$$

$$\therefore M(-1.678, 0.096)$$

3 d.p

- c) AS CONVERGENCE TAKES PLACE BY OSCILLATIONS,  
WE HAVE A "COBWEB" TYPE DIAGRAM

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## IYGB - MP2 PAPER 7 - QUESTION 7

$$f(x) = \frac{e^{\sqrt[4]{x}}}{\sqrt{x}}, \quad x > 0$$

USING THE SUBSTITUTION GIVEN WE HAVE

$$\begin{aligned} u &= \sqrt[4]{x} = x^{\frac{1}{4}} & \text{and} & & x=0 & \mapsto & 0 \\ u^2 &= \sqrt{x} = x^{\frac{1}{2}} & & & x=1 & \mapsto & 1 \\ u^4 &= x \end{aligned}$$

$$\frac{dx}{du} = 4u^3$$

TRANSFORMING THE INTEGRAL WE HAVE

$$\int_0^1 \frac{e^{\sqrt[4]{x}}}{\sqrt{x}} dx = \int_0^1 \frac{e^u}{u^2} (4u^3) = \int_0^1 4ue^u du$$

INTEGRATION BY PARTS FOLLOWS (IGNORING LIMITS)

$$\begin{array}{c|c} 4u & 4 \\ \hline e^u & e^u \end{array} \Rightarrow \int 4ue^u du = 4ue^u - \int 4e^u du \\ = 4ue^u - 4e^u + C \\ = 4e^u(u-1) + C$$

INSERTING THE LIMITS AND EVALUATING

$$\begin{aligned} \int_0^1 4ue^u du &= [4e^u(u-1)]_0^1 = \cancel{4e^1(1-1)} - 4e^0(0-1) \\ &= \underline{4} \end{aligned}$$

1YGB - MP2 PAPER P - QUESTION 8

a) CREATE A "ONE" AND "EXPAND"

$$\begin{aligned} \left(\frac{1}{4} - x\right)^{-\frac{3}{2}} &= \left(\frac{1}{4}\right)^{-\frac{3}{2}} (1 - 4x)^{-\frac{3}{2}} = 4^{\frac{3}{2}} (1 - 4x)^{-\frac{3}{2}} \\ &= 8 [1 - 4x]^{-\frac{3}{2}} \\ &= 8 \left[ 1 + \frac{-\frac{3}{2}}{1!} (-4x)^1 + \frac{-\frac{3}{2}(-\frac{3}{2})}{2!} (-4x)^2 + \frac{(-\frac{3}{2})(-\frac{5}{2})(-\frac{7}{2})}{3!} (-4x)^3 + \dots \right] \\ &= 8 [1 + 6x + 30x^2 + 140x^3 + \dots] \\ &= \underline{\underline{8 + 48x + 240x^2 + 1120x^3 + \dots}} \end{aligned}$$

b) PROCES AS BINOMIALS

$$\begin{aligned} \sqrt{\frac{1}{4} - x} &= \left(\frac{1}{4} - x\right)^{\frac{1}{2}} = \left(\frac{1}{4} - x\right)^2 \left(\frac{1}{4} - x\right)^{-\frac{3}{2}} \\ &= \left(\frac{1}{16} - \frac{1}{2}x + x^2\right) (8 + 48x + 240x^2 + 1120x^3 + \dots) \\ &= \frac{1}{2} + 3x + 15x^2 + 70x^3 + \dots \\ &\quad - 4x - 24x^2 - 120x^3 + \dots \\ &\quad \underline{\quad 8x^2 + 48x^3 + \dots} \\ &= \underline{\underline{\frac{1}{2} - x - x^2 - 2x^3 + \dots}} \end{aligned}$$

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## 1YGB - MP2 PAPER P - QUESTION 9

START BY RELATING DERIVATIVES

$$\Rightarrow \frac{dh}{dt} = \frac{dh}{dV} \times \frac{dV}{dt}$$

$$\Rightarrow \frac{dh}{dt} = \frac{dh}{dU} \times 5$$



WE NEED TO DIFFERENTIATE A FORMULA WHICH CONNECTS  $h$  &  $V$

$$\Rightarrow V = -2 + (2h^3 + 3h + 8)^{\frac{1}{2}}$$

$$\Rightarrow \frac{dV}{dh} = 0 + \frac{1}{2}(2h^3 + 3h + 8)^{-\frac{1}{2}} \times (6h^2 + 3)$$

$$\Rightarrow \frac{dV}{dh} = \frac{6h^2 + 3}{2(2h^3 + 3h + 8)^{\frac{1}{2}}}$$

$$\Rightarrow \frac{dh}{dU} = \frac{2(2h^3 + 3h + 8)^{\frac{1}{2}}}{6h^2 + 3}$$

RETURNING TO THE "MAIN UNIT"

$$\Rightarrow \frac{dh}{dt} = \frac{2(2h^3 + 3h + 8)^{\frac{1}{2}}}{6h^2 + 3} \times 5$$

$$\Rightarrow \left. \frac{dh}{dt} \right|_{h=11} = \frac{10(2 \times 11^3 + 3 \times 11 + 8)^{\frac{1}{2}}}{6 \times 11^2 + 3}$$

$$\Rightarrow \left. \frac{dh}{dt} \right|_{h=11} = 0.713173988 \dots \approx \underline{0.713 \text{ cm s}^{-1}}$$

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# IYGB - MP2 PAPER P - QUESTION 10

START BY REARRANGING THE RELATIONSHIP

$$\Rightarrow \tan 3y = 3 \tan x$$

$$\Rightarrow 3y = \arctan(3 \tan x) \pm n\pi \quad n=0,1,2,3,\dots$$

$$\Rightarrow y = \frac{1}{3} \arctan(3 \tan x) \pm \frac{n\pi}{3}$$

USING THE GIVEN RESULT  $\frac{d}{dx}(\arctan x) = \frac{1}{x^2+1}$  WE OBTAIN

$$\Rightarrow \frac{dy}{dx} = \frac{1}{3} \times \frac{1}{(3 \tan x)^2 + 1} \times \frac{d}{dx}(3 \tan x)$$

$$\Rightarrow \frac{dy}{dx} = \cancel{\frac{1}{3}} \times \frac{1}{9 \tan^2 x + 1} \times \cancel{3} \sec^2 x$$

$$\Rightarrow \frac{dy}{dx} = \frac{\sec^2 x}{9 \tan^2 x + 1}$$

$$\Rightarrow \frac{dy}{dx} = \frac{\frac{1}{\cos^2 x}}{\frac{9 \sin^2 x}{\cos^2 x} + 1}$$

MULTIPLY "TOP & BOTTOM" OF THE FRACTION BY  $\cos^2 x$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{9 \sin^2 x + \cos^2 x}$$

$$\Rightarrow \frac{dy}{dx} = \frac{1}{8 \sin^2 x + (\sin^2 x + \cos^2 x)}$$

$$= \frac{1}{\underline{8 \sin^2 x + 1}}$$

is simplified

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1YGB - MP2 PAPER P - QUESTION 10

ALTERNATIVE BY IMPLICIT DIFFERENTIATION

$$\Rightarrow \tan 3y = 3 \tan x$$

$$\Rightarrow \frac{d}{dx}(\tan 3y) = \frac{d}{dx}(3 \tan x)$$

$$\Rightarrow 3 \sec^2 3y \frac{dy}{dx} = 3 \sec^2 x$$

$$\Rightarrow \frac{dy}{dx} = \frac{\sec^2 x}{\sec^2 3y}$$

ELIMINATE  $y$  IN THE R.H.S BY USING  $1 + \tan^2 3y \equiv \sec^2$

$$\Rightarrow \frac{dy}{dx} = \frac{\sec^2 x}{1 + \tan^2 3y}$$

$$\Rightarrow \frac{dy}{dx} = \frac{\sec^2 x}{1 + (3 \tan x)^2}$$

q THE SOLUTION MERGES WITH THE METHOD  
PREVIOUSLY USED ...

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## IYGB - NP2 PAPER 7 - QUESTION 11

STARTING FROM THE SECOND EQUATION

$$\Rightarrow \tan \theta + \tan \phi = 3$$

$$\Rightarrow \frac{\sin \theta}{\cos \theta} + \frac{\sin \phi}{\cos \phi} = 3$$

$$\Rightarrow \frac{\sin \theta \cos \phi + \sin \phi \cos \theta}{\cos \theta \cos \phi} = 3$$

$$\Rightarrow \sin \theta \cos \phi + \sin \phi \cos \theta = 3 \cos \theta \cos \phi$$

$$\Rightarrow \sin(\theta + \phi) = 3 \cos \theta \cos \phi$$

NOW THE FIRST EQUATION SIMPLIFIES

$$\Rightarrow \sin^2 \alpha + 2 \sin \alpha + \cancel{\sin(\theta + \phi)} = \cancel{3 \cos \theta \cos \phi} - 1$$

$$\Rightarrow \sin^2 \alpha + 2 \sin \alpha = -1$$

$$\Rightarrow \sin^2 \alpha + 2 \sin \alpha + 1 = 0$$

$$\Rightarrow (\sin \alpha + 1)^2 = 0$$

$$\Rightarrow \underline{\underline{\sin \alpha = -1}}$$

AS REQUIRED

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# 1YGB - MP2 PAPER P - QUESTION 12

a) WE START WITH THE DOMAIN OF  $f(g(x))$



THE DOMAIN MUST SATISFY

$$x \leq 10 \quad \text{AND} \quad \begin{aligned} x-6 &\geq 1 \\ x &\geq 7 \end{aligned}$$

COMBINING WE OBTAIN

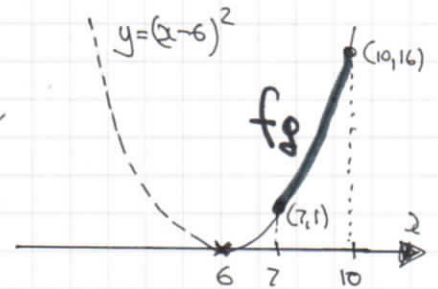
$$7 \leq x \leq 10$$

TO FIND THE RANGE

$$f(g(x)) = f(x-6) = (x-6)^2$$

SKETCHING NOTING THE DOMAIN

$$\therefore 1 \leq f(g(x)) \leq 16$$



b) SOLVING THE EQUATION

$$\Rightarrow f(g(x)) = g^{-1}(x)$$

$$\Rightarrow (x-6)^2 = x+6$$

$$\Rightarrow x^2 - 12x + 36 = x + 6$$

$$\begin{aligned} g(x) &= x-6 \\ y &= x-6 \\ y+6 &= x \\ g^{-1}(x) &= x+6 \end{aligned}$$

IYGB - MP2 PAPER 1 - QUESTION 12

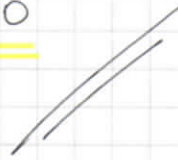
$$\Rightarrow x^2 - 13x + 30 = 0$$

$$\Rightarrow (x - 10)(x - 3) = 0$$

$$\Rightarrow x = \begin{cases} 3 \\ 10 \end{cases}$$

LOOKING AT THE DOMAIN OF  $f(g(x))$

ONLY SOLUTION IS  $x = 10$



# LYGB - MP2 PAPER P - QUESTION 13

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a) OBTAIN THE GRADIENT FUNCTION IN PARAMETRIC

$$\frac{dy}{dx} = \frac{dy/d\theta}{dx/d\theta} = \frac{2\cos 2\theta + \sin \theta}{-\sin \theta}$$

$$\left. \frac{dy}{dx} \right|_{\theta = \frac{\pi}{4}} = \frac{2\cos \frac{\pi}{2} + \sin \frac{\pi}{4}}{-\sin \frac{\pi}{4}} = \frac{0 + \frac{\sqrt{2}}{2}}{-\frac{\sqrt{2}}{2}} = -1$$

with  $\theta = \frac{\pi}{4}$

$$\left. \begin{aligned} \bullet x &= \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2} \\ \bullet y &= \sin \frac{\pi}{2} - \cos \frac{\pi}{4} = 1 - \frac{\sqrt{2}}{2} \end{aligned} \right\} \text{ i.e. } \left( \frac{\sqrt{2}}{2}, 1 - \frac{\sqrt{2}}{2} \right)$$

finally we have

$$y - y_0 = m(x - x_0)$$

$$y - \left(1 - \frac{\sqrt{2}}{2}\right) = -1 \left(x - \frac{\sqrt{2}}{2}\right)$$

$$y - 1 + \frac{\sqrt{2}}{2} = -x + \frac{\sqrt{2}}{2}$$

$$y + x = 1$$

b) Now at  $\theta = \frac{\pi}{4}$

$$\left. \frac{dy}{dx} \right|_{\theta = \frac{\pi}{4}} = \frac{2\cos \frac{\pi}{2} + \sin \frac{\pi}{4}}{-\sin \frac{\pi}{4}} = \frac{0 - \frac{\sqrt{2}}{2}}{\frac{\sqrt{2}}{2}} = -1$$

$$\left. \begin{aligned} \bullet x &= \cos \frac{\pi}{4} = \frac{\sqrt{2}}{2} \\ \bullet y &= \sin \frac{\pi}{2} - \cos \frac{\pi}{4} = 1 - \frac{\sqrt{2}}{2} \end{aligned} \right\} \text{ i.e. } \left( \frac{\sqrt{2}}{2}, 1 - \frac{\sqrt{2}}{2} \right)$$

FORMING TANGENT EQUATION AT POINT WITH  $\theta = \frac{\pi}{4}$

$$y - y_0 = m(x - x_0)$$

$$y - \left(1 - \frac{\sqrt{2}}{2}\right) = -1 \left(x - \frac{\sqrt{2}}{2}\right)$$

$$y - 1 + \frac{\sqrt{2}}{2} = -x + \frac{\sqrt{2}}{2}$$

$$\underline{y + x = 1}$$

~~same line~~

1YGB - MP2 PAPER P - QUESTION 13

c) WE ELIMINATE BY MANIPULATING THE "y EQUATION"

$$\Rightarrow y = \sin 2\theta - \cos \theta$$

$$\Rightarrow y = 2\sin \theta \cos \theta - \cos \theta$$

$$\Rightarrow y = (2\sin \theta - 1) \cos \theta$$

$$\Rightarrow \frac{y}{\cos \theta} = 2\sin \theta - 1$$

$$\Rightarrow \frac{y}{\cos \theta} + 1 = 2\sin \theta$$

$$\Rightarrow \frac{y}{2} + 1 = 2\sin \theta$$

$$\Rightarrow \frac{y+2}{2} = 2\sin \theta$$

$$\Rightarrow \frac{(y+2)^2}{2^2} = 4\sin^2 \theta$$

$$\Rightarrow \frac{(y+2)^2}{2^2} = 4(1 - \cos^2 \theta)$$

$$\Rightarrow \frac{(y+2)^2}{2^2} = 4(1 - x^2)$$

$$\Rightarrow \underline{(y+2)^2 = 4x^2(1-x^2)}$$

AS REQUIRED